

Table I—Transfer Functions of R-C Input and Output Networks

To generate a specific  $f(p)$ , rewrite  $f(p)$  in the form  $Z_o/Z_i$  where  $Z_o$  and  $Z_i$  are each in a form correspond-

ing to a function in the left-hand column. Choose input and output networks in accordance with the diagrams and relations

adjacent to the function representing  $Z_i$  and  $Z_o$  respectively.

TRANSFER IMPEDANCE FUNCTION	NETWORK	RELATIONS	INVERSE RELATIONS	TRANSFER IMPEDANCE FUNCTION	NETWORK	RELATIONS	INVERSE RELATIONS
A		A = R	R = A	$\frac{1}{pB} (1+pT_1)(1+pT_2)$		B = C <sub>2</sub> T <sub>1</sub> T <sub>2</sub> = R <sub>1</sub> R <sub>2</sub> C <sub>1</sub> C <sub>2</sub> T <sub>1</sub> + T <sub>2</sub> = R <sub>1</sub> C <sub>1</sub> + R <sub>2</sub> C <sub>2</sub> + R <sub>1</sub> C <sub>2</sub>	$R_1 = \frac{(\sqrt{T_1} - \sqrt{T_2})^2}{B}$ $R_2 = \frac{\sqrt{T_1 T_2}}{B}$ $C_1 = \frac{B\sqrt{T_1 T_2}}{(\sqrt{T_1} - \sqrt{T_2})^2}$ C <sub>2</sub> = B
$\frac{A}{1+pT}$		A = R T = RC	R = A C = $\frac{T}{A}$	$\frac{1}{pB} \left[ \frac{(1+pT_1)(1+pT_2)}{p\sqrt{T_1 T_2}} \right]$		B = C <sub>2</sub> T <sub>1</sub> T <sub>2</sub> = R <sub>1</sub> R <sub>2</sub> C <sub>1</sub> C <sub>2</sub> T <sub>1</sub> + T <sub>2</sub> = R <sub>1</sub> C <sub>1</sub> + R <sub>2</sub> C <sub>2</sub> + R <sub>1</sub> C <sub>2</sub>	$R = \frac{(\sqrt{T_1} - \sqrt{T_2})^2}{B}$ $R_2 = \frac{\sqrt{T_1 T_2}}{B}$ $C_1 = \frac{B\sqrt{T_1 T_2}}{(\sqrt{T_1} - \sqrt{T_2})^2}$ C <sub>2</sub> = B
A(1+pT)		A = 2R T = $\frac{RC}{2}$	R = $\frac{A}{2}$ C = $\frac{4T}{A}$	$\frac{1}{pB} \left[ \frac{(1+pT_1)(1+pT_2)}{p^2\sqrt{T_1 T_2}} \right]$		B = C <sub>2</sub> T <sub>1</sub> T <sub>2</sub> = R <sub>1</sub> R <sub>2</sub> C <sub>1</sub> C <sub>2</sub> T <sub>1</sub> + T <sub>2</sub> = R <sub>1</sub> C <sub>1</sub> + R <sub>2</sub> C <sub>2</sub> + R <sub>1</sub> C <sub>2</sub>	$R = \frac{(\sqrt{T_1} - \sqrt{T_2})^2}{B}$ $R_2 = \frac{\sqrt{T_1 T_2}}{B}$ $C_1 = \frac{B\sqrt{T_1 T_2}}{(\sqrt{T_1} - \sqrt{T_2})^2}$ C <sub>2</sub> = B
$A \left( \frac{1+p\theta T}{1+pT} \right)$		A = R <sub>1</sub> + R <sub>2</sub> T = R <sub>2</sub> C $\theta = \frac{R_1}{R_1 + R_2}$	R <sub>1</sub> = Aθ R <sub>2</sub> = A(1-θ) C = $\frac{T}{A(1-\theta)}$	$\frac{1}{pB} \left[ \frac{(1+pT_1)(1+pT_2)}{p^2\sqrt{T_1 T_2}} \right]$		B = $\frac{C_1 C_2}{C_1 + 2C_2}$ T <sub>1</sub> = RC <sub>1</sub> T <sub>2</sub> = R(C <sub>1</sub> + 2C <sub>2</sub> )	R = $\frac{T_1(T_2 - T_1)}{2BT_2}$ C <sub>1</sub> = $\frac{2BT_2}{T_2 - T_1}$ C <sub>2</sub> = $\frac{BT_2}{T_1}$
		A = R <sub>1</sub> T = (R <sub>1</sub> + R <sub>2</sub> )C $\theta = \frac{R_2}{R_1 + R_2}$	R <sub>1</sub> = A R <sub>2</sub> = $\frac{A\theta}{1-\theta}$ C = $\frac{T(1-\theta)}{A}$				
$A \left( \frac{1+pT}{1+p\theta T} \right)$		A = $\frac{2R_1 R_2}{2R_1 + R_2}$ T = $\frac{R_1 C}{2}$ $\theta = \frac{2R_1}{2R_1 + R_2}$	R <sub>1</sub> = $\frac{A}{2(1-\theta)}$ R <sub>2</sub> = $\frac{A\theta}{1-\theta}$ C = $\frac{4T(1-\theta)}{A}$	$A \left( \frac{1+pT_1}{1+p^2 T_1 T_2} \right)$		A = 2R <sub>1</sub> T <sub>1</sub> = $\frac{R_1 C_1}{2} = 2R_2 C_2$ T <sub>2</sub> = R <sub>1</sub> C <sub>2</sub> R <sub>1</sub> C <sub>1</sub> = 4R <sub>2</sub> C <sub>2</sub>	R <sub>1</sub> = $\frac{A}{2}$ R <sub>2</sub> = $\frac{AT_1}{4T_2}$ C <sub>1</sub> = $\frac{4T_1}{A}$ C <sub>2</sub> = $\frac{2T_2}{A}$
		A = 2R <sub>1</sub> T = $\left( R_2 + \frac{R_1}{2} \right) C$ $\theta = \frac{2R_2}{2R_2 + R_1}$	R <sub>1</sub> = $\frac{A}{2}$ R <sub>2</sub> = $\frac{A\theta}{4(1-\theta)}$ C = $\frac{4T(1-\theta)}{A}$				
		A = 2R T = $\frac{R}{2} (C_1 + C_2)$ $\theta = \frac{2C_2}{C_1 + C_2}$	R = $\frac{A}{2}$ C <sub>1</sub> = $\frac{2T(2-\theta)}{A}$ C <sub>2</sub> = $\frac{2T\theta}{A}$				
$\frac{1}{pB} \left[ \frac{(1+pT_1)(1+pT_2)(1+pT_3)}{1+pT_2} \right]$		B = C <sub>1</sub> T <sub>2</sub> = (R <sub>1</sub> + R <sub>2</sub> )C <sub>2</sub> T <sub>1</sub> T <sub>3</sub> = R <sub>1</sub> R <sub>2</sub> C <sub>1</sub> C <sub>2</sub> T <sub>1</sub> + T <sub>3</sub> = R <sub>1</sub> C <sub>1</sub> + R <sub>2</sub> C <sub>2</sub> + R <sub>1</sub> C <sub>2</sub>	R <sub>1</sub> = $\frac{T_1 + T_3 - T_2}{B}$ R <sub>2</sub> = $\frac{T_1 T_3 (T_1 + T_3 - T_2)}{B(T_3 - T_2)(T_2 - T_1)}$ C <sub>1</sub> = B C <sub>2</sub> = $\frac{B(T_3 - T_2)(T_2 - T_1)}{(T_1 + T_3 - T_2)^2}$	$\frac{1}{pB} \left( \frac{1+pT}{pT} \right)$		B = $\frac{C}{2}$ T = 2RC	R = $\frac{T}{4B}$ C = 2B
		B = C <sub>1</sub> C <sub>2</sub> T <sub>2</sub> = R <sub>2</sub> $\left( \frac{C_1 C_2}{C_1 + C_2} \right)$ T <sub>1</sub> T <sub>3</sub> = R <sub>1</sub> R <sub>2</sub> C <sub>1</sub> C <sub>2</sub> T <sub>1</sub> + T <sub>3</sub> = R <sub>1</sub> C <sub>1</sub> + R <sub>2</sub> C <sub>2</sub> + R <sub>1</sub> C <sub>2</sub>	R <sub>1</sub> = $\frac{T_1 T_3}{BT_2}$ R <sub>2</sub> = $\frac{(T_1 T_2 + T_2 T_3 - T_1 T_3)^2}{BT_2(T_3 - T_2)(T_2 - T_1)}$ C <sub>1</sub> = $\frac{BT_2^2}{T_1 T_2 + T_2 T_3 - T_1 T_3}$ C <sub>2</sub> = $\frac{B(T_3 - T_2)(T_2 - T_1)}{T_1 T_2 + T_2 T_3 - T_1 T_3}$				
		B = C <sub>1</sub> T <sub>2</sub> = R <sub>2</sub> C <sub>2</sub> T <sub>1</sub> T <sub>3</sub> = R <sub>1</sub> R <sub>2</sub> C <sub>1</sub> C <sub>2</sub> T <sub>1</sub> + T <sub>3</sub> = R <sub>1</sub> C <sub>1</sub> + R <sub>2</sub> C <sub>2</sub> + R <sub>1</sub> C <sub>2</sub>	R <sub>1</sub> = $\frac{T_1 T_3}{BT_2}$ R <sub>2</sub> = $\frac{(T_3 - T_2)(T_2 - T_1)}{BT_2}$ C <sub>1</sub> = B C <sub>2</sub> = $\frac{BT_2^2}{(T_3 - T_2)(T_2 - T_1)}$				
		B = C <sub>1</sub> C <sub>2</sub> T <sub>2</sub> = R <sub>2</sub> $\left( \frac{C_1 C_2}{C_1 + C_2} \right)$ T <sub>1</sub> T <sub>3</sub> = R <sub>1</sub> R <sub>2</sub> C <sub>1</sub> C <sub>2</sub> T <sub>1</sub> + T <sub>3</sub> = R <sub>1</sub> C <sub>1</sub> + R <sub>2</sub> C <sub>2</sub> + R <sub>1</sub> C <sub>2</sub>	R = $\frac{T}{B(1-\theta)}$ C <sub>1</sub> = B C <sub>2</sub> = $\frac{B\theta}{1-\theta}$ C <sub>2</sub> = B(1-θ)				
		B = C <sub>1</sub> T <sub>2</sub> = R <sub>2</sub> C <sub>2</sub> T <sub>1</sub> T <sub>3</sub> = R <sub>1</sub> R <sub>2</sub> C <sub>1</sub> C <sub>2</sub> T <sub>1</sub> + T <sub>3</sub> = R <sub>1</sub> C <sub>1</sub> + R <sub>2</sub> C <sub>2</sub> + R <sub>1</sub> C <sub>2</sub>	R = $\frac{T}{B(1-\theta)}$ C <sub>1</sub> = Bθ C <sub>2</sub> = B(1-θ)				
$\frac{1}{pB} \left[ \frac{(1+pT_1)(1+pT_2)(1+pT_3)}{1+pT_2} \right]$		B = C <sub>1</sub> C <sub>2</sub> T <sub>2</sub> = (R <sub>1</sub> + R <sub>2</sub> ) $\left( \frac{C_1 C_2}{C_1 + C_2} \right)$ T <sub>1</sub> T <sub>3</sub> = R <sub>1</sub> R <sub>2</sub> C <sub>1</sub> C <sub>2</sub> T <sub>1</sub> + T <sub>3</sub> = R <sub>1</sub> C <sub>1</sub> + R <sub>2</sub> C <sub>2</sub> + R <sub>1</sub> C <sub>2</sub>	R <sub>1</sub> = $\frac{T_1 T_3}{BT_2}$ R <sub>2</sub> = $\frac{(T_3 - T_2)(T_2 - T_1)}{BT_2}$ C <sub>1</sub> = B C <sub>2</sub> = $\frac{BT_2^2}{(T_3 - T_2)(T_2 - T_1)}$	$\frac{1}{pB} \left[ \frac{(1+pT_1)(1+pT_2)(1+pT_3)}{1+pT_2} \right]$		B = C <sub>1</sub> + C <sub>2</sub> T <sub>1</sub> = R <sub>1</sub> C <sub>1</sub> T <sub>2</sub> = (R <sub>1</sub> + R <sub>2</sub> ) $\left( \frac{C_1 C_2}{C_1 + C_2} \right)$ T <sub>3</sub> = R <sub>2</sub> C <sub>2</sub>	R <sub>1</sub> = $\frac{T_1(T_3 - T_1)}{B(T_2 - T_1)}$ R <sub>2</sub> = $\frac{T_3(T_3 - T_1)}{B(T_3 - T_2)}$ C <sub>1</sub> = $\frac{B(T_2 - T_1)}{T_3 - T_1}$ C <sub>2</sub> = $\frac{B(T_3 - T_2)}{T_3 - T_1}$
$T_1 < T_2 < T_3$	$T_1 < T_2 < T_3$						

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Table I (continued)—Transfer Functions of R-C Input and Output Networks

TRANSFER IMPEDANCE FUNCTION	NETWORK	RELATIONS	INVERSE RELATIONS
$A \frac{1+pT_1}{1+pT_1+p^2T_1T_2}$		$A = R_2$ $T_1 = 2R_1C$ $T_2 = \frac{R_2C}{2}$	$R_1 = \frac{AT_1}{4T_2}$ $R_2 = A$ $C = \frac{2T_2}{A}$
$A \frac{1+pT_2}{1+pT_1+p^2T_1T_2}$		$A = 2R$ $T_1 = 2RC_2$ $T_2 = \frac{RC_1}{2}$	$R = \frac{A}{2}$ $C_1 = \frac{4T_2}{A}$ $C_2 = \frac{T_1}{A}$
$A \frac{1+pT_3}{1+pT_1+p^2T_1T_2}$ $T_2 > \frac{T_1}{4}$ (Complex roots) $T_3 > T_2$		$A = \frac{2R_1R_2}{2R_1+R_2}$ $T_1 = \frac{R_1(R_1C_1+2R_2C_2)}{2R_1+R_2}$ $T_2 = \frac{R_1R_2C_1C_2}{R_1C_1+2R_2C_2}$ $T_3 = \frac{R_1C_1}{2}$	$R_1 = \frac{AT_3^2}{2[T_3^2-T_1(T_3-T_2)]}$ $R_2 = \frac{AT_3^2}{T_1(T_3-T_2)}$ $C_1 = \frac{4[T_3^2-T_1(T_3-T_2)]}{AT_3}$ $C_2 = \frac{T_1T_2}{AT_3}$
		$A = 2R_1$ $T_1 = R_2C_1+2R_1C_2$ $T_2 = \frac{R_1(R_1+2R_2)C_1C_2}{R_2C_1+2R_1C_2}$ $T_3 = \left(R_2 + \frac{R_1}{2}\right)C_1$	$R_1 = \frac{A}{2}$ $R_2 = \frac{AT_1(T_3-T_2)}{4[T_3^2-T_1(T_3-T_2)]}$ $C_1 = \frac{4[T_3^2-T_1(T_3-T_2)]}{AT_3}$ $C_2 = \frac{T_1T_2}{AT_3}$
		$A = 2R$ $T_1 = R(C_2+2C_3)$ $T_2 = \frac{RC_3(C_1+C_2)}{C_2+2C_3}$ $T_3 = \frac{R}{2}(C_1+C_2)$	$R = \frac{A}{2}$ $C_1 = \frac{2[2T_3^2-T_1(T_3-T_2)]}{AT_3}$ $C_2 = \frac{2T_1(T_3-T_2)}{AT_3}$ $C_3 = \frac{T_1T_2}{AT_3}$
$A \frac{1+pT_3}{1+pT_1+p^2T_1T_2}$ $T_2 > \frac{T_1}{4}$ (Complex roots) $T_3 < T_1$		$A = R_2$ $T_1 = 2R_1C_1+R_2C_2$ $T_2 = \frac{R_1R_2C_1(C_1+2C_2)}{2R_1C_1+R_2C_2}$ $T_3 = 2R_1C_1$	$R_1 = \frac{AT_3^2}{4(T_1T_2-T_3(T_1-T_3))}$ $R_2 = A$ $C_1 = \frac{2(T_1T_2-T_3(T_1-T_3))}{AT_3}$ $C_2 = \frac{(T_1-T_3)}{A}$
		$A = R_2$ $T_1 = \frac{C_1(2R_1C_2+R_2C_1)}{2C_1+C_2}$ $T_2 = \frac{R_1R_2C_1C_2}{2R_1C_2+R_2C_1}$ $T_3 = \frac{2R_1C_1C_2}{2C_1+C_2}$	$R_1 = \frac{AT_3^2}{4(T_1T_2-T_3(T_1-T_3))}$ $R_2 = A$ $C_1 = \frac{2T_1T_2}{AT_3}$ $C_2 = \frac{4T_1T_2(T_1T_2-T_3(T_1-T_3))}{AT_3^2(T_1-T_3)}$
		$A = R_3$ $T_1 = \frac{R_1(2R_2+R_3)C}{R_1+R_2}$ $T_2 = \frac{R_2R_3C}{2R_2+R_3}$ $T_3 = \frac{2R_1R_2C}{(R_1+R_2)}$	$R_1 = \frac{AT_3^2}{2[2T_1T_2-T_3(T_1-T_3)]}$ $R_2 = \frac{AT_3}{2(T_1-T_3)}$ $R_3 = A$ $C = \frac{2T_1T_2}{AT_3}$
$A(1+pT_1)(1+pT_2)$ $T_1 < T_2$		$A = 2R_1+R_2$ $T_1 = \left(\frac{R_1R_2}{2R_1+R_2}\right)C$ $T_2 = R_1C$	$R_1 = A \frac{T_2-T_1}{2T_2}$ $R_2 = A \frac{T_1}{T_2}$ $C = \frac{2T_2^2}{A(T_2-T_1)}$

TRANSFER IMPEDANCE FUNCTION	NETWORK	RELATIONS	INVERSE RELATIONS
$\frac{1}{pB} \frac{1+p\theta T}{1+pT}$ $\theta < 1$		$B = C_2$ $T = RC_1 \left(\frac{2C_2+C_1}{C_2}\right)$ $\theta = \frac{2C_2}{2C_2+C_1}$	$R = \frac{T\theta^2}{4B(1-\theta)}$ $C_1 = \frac{2B(1-\theta)}{\theta}$ $C_2 = B$
$A \frac{1+pT_2}{(1+pT_1)(1+pT_3)}$ $T_1 < T_2 < T_3$		$B = \frac{C_1^2}{2C_1+C_2}$ $T = RC_2$ $\theta = \frac{2C_1}{2C_1+C_2}$	$R = \frac{T\theta^2}{4B(1-\theta)}$ $C_1 = \frac{2B}{\theta}$ $C_2 = \frac{4B(1-\theta)}{\theta^2}$
		$B = \left(\frac{R_1}{R_1+R_2}\right)C$ $T = R_2C$ $\theta = \frac{2R_1}{R_1+R_2}$	$R_1 = \frac{T\theta^2}{2B(2-\theta)}$ $R_2 = \frac{T\theta}{2B}$ $C = \frac{2B}{\theta}$
		$A = R_1+R_2$ $T_1 = R_1C_1$ $T_2 = \left(\frac{R_1R_2}{R_1+R_2}\right)(C_1+C_2)$ $T_3 = R_2C_2$	$R_1 = \frac{A(T_2-T_1)}{T_3-T_1}$ $R_2 = \frac{A(T_3-T_2)}{T_3-T_1}$ $C_1 = \frac{T_1(T_3-T_1)}{A(T_2-T_1)}$ $C_2 = \frac{T_3(T_3-T_1)}{A(T_3-T_2)}$
$A \frac{1+pT_2}{(1+pT_1)(1+pT_3)}$ $T_2 < T_1 < T_3$		$A = R_2$ $T_2 = R_1C_1$ $T_1T_3 = R_1R_2C_1C_2$ $T_1+T_3 = R_1C_1+R_2C_2+R_2C_1$	$R_1 = \frac{AT_2^2}{(T_3-T_2)(T_2-T_1)}$ $R_2 = A$ $C_1 = \frac{(T_3-T_2)(T_2-T_1)}{AT_2}$ $C_2 = \frac{T_1T_3}{AT_2}$
		$A = R_1+R_2$ $T_2 = \left(\frac{R_1R_2}{R_1+R_2}\right)C_2$ $T_1T_3 = R_1R_2C_1C_2$ $T_1+T_3 = R_1C_1+R_2C_2+R_2C_1$	$R_1 = \frac{AT_2^2}{T_1T_2+T_2T_3-T_1T_3}$ $R_2 = \frac{A(T_3-T_2)(T_2-T_1)}{T_1T_2+T_2T_3-T_1T_3}$ $C_1 = \frac{T_1T_3}{AT_2}$ $C_2 = \frac{(T_1T_2+T_2T_3-T_1T_3)^2}{AT_2(T_3-T_2)(T_2-T_1)}$
		$A = R_1$ $T_2 = R_2(C_1+C_2)$ $T_1T_3 = R_1R_2C_1C_2$ $T_1+T_3 = R_1C_1+R_2C_2+R_2C_1$	$R_1 = A$ $R_2 = \frac{A(T_3-T_2)(T_2-T_1)}{(T_1+T_3-T_2)^2}$ $C_1 = \frac{T_1+T_3-T_2}{A}$ $C_2 = \frac{T_1T_3(T_1+T_3-T_2)}{A(T_3-T_2)(T_2-T_1)}$
$A \frac{1+pT_2}{(1+pT_1)(1+pT_3)}$ $T_2 < T_1 < T_3$		$A = 2R_1 + \frac{R_1^2}{R_2}$ $T_1 = R_1C_1$ $T_2 = \left(\frac{R_1R_2}{R_1+2R_2}\right)(C_1+C_2)$ $T_3 = R_1C_2$	$R_1 = \frac{AT_2}{(T_1+T_3)}$ $R_2 = \frac{AT_2^2}{(T_1+T_3)(T_1+T_3-2T_2)}$ $C_1 = \frac{T_1(T_1+T_3)}{AT_2}$ $C_2 = \frac{T_3(T_1+T_3)}{AT_2}$
$A \frac{1+pT_2}{(1+pT_1)(1+pT_3)}$ $T_1 < T_3 < T_2$		$A = R_1+R_2$ $T_1 = R_1C_1$ $T_2 = \frac{R_1R_2}{R_1+R_2}(2C_1+C_2)$ $T_3 = R_2C_1$	$R_1 = \frac{AT_1}{(T_1+T_3)}$ $R_2 = \frac{AT_3}{(T_1+T_3)}$ $C_1 = \frac{(T_1+T_3)}{A}$ $C_2 = \frac{(T_1+T_3)}{A} \left(\frac{T_2}{T_3} - \frac{T_2-T_1}{T_3-T_1}\right)$